

# CS 134

## Video Game Math

Game Engine Architecture  
Chapter 4

# Today in Video Games



Twin Galaxies Adjudication Issues Statement In  
Regard To Billy Mitchell Donkey Kong Dispute



by Twin Galaxies Editorial Staff, February 2, 2018 4:55 PM

More add codes

Homework questions?

# Video Game Math



While the game is running, guys are moving around.

Where are they at any point in time?

When you click, which tile got clicked on?

# Video Game Math

- Algebra, Linear Algebra, Geometry, and Trigonometry are the common maths of Video Games.
  - And a smidge of basic Calculus... just a smidge!
- Let's do a review of the math needed when writing games.

# Video Game Math



# Video Game Math

- Algebra and Geometry
  - Algebra – Solve for X:  $X^2 + 6 = 10$
  - Geometry – Properties of Circles, Triangles
- Pythagorean Theorem
- Quadratic Formula
- Simple motion



# Video Game Math

- How long would it take to move from Start to End?
- Assume speed of 30px / second.



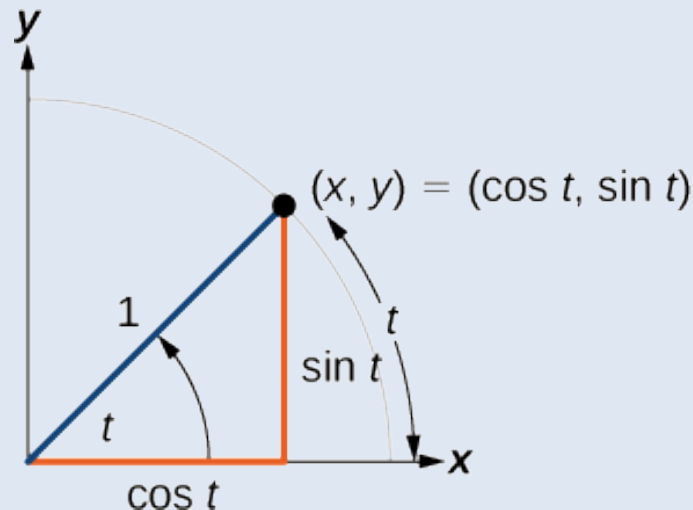
# Video Game Math

- How long would it take to move from Start to End?
- Assume speed of 30px / second.
- Needed info:
  - Delta X = 4 tiles
  - Delta Y = 2 tiles
  - 1 tile = 16x16 pixels



# Video Game Math

- Trigonometry
  - Sin, Cos, Tan as the circle functions
- $\cos^2(x) + \sin^2(x) = 1$
- atan2, one of the most useful functions.



# Video Game Math

- What angle should the character be rotated to face the direction they are walking?
- Remember:
  - Delta X = 4 tiles
  - Delta Y = 2 tiles
  - 1 tile = 16x16 pixels



# Video Game Math

- Viewing these operations as doing Linear Algebra makes a lot of the operations easier.
- Linear Algebra according to MathWorld is:
  - The study of linear systems of equations and their transformation properties.
- This is **NOT** the way game developers view Linear Algebra.

# Video Game Math

- Viewing these operations as doing Linear Algebra makes a lot of the operations easier.
- Linear Algebra according to game devs is:
  - The study of 2D and 3D positions and how they change in different views.

# Video Game Math

- Video Game Linear Algebra:
  - Instead of viewing the world as having X values and Y values, view the world as a collection of (X,Y) values.
    - This is a POINT or a VECTOR.
  - A transformation to another view of the world is represented as a collection of new values for the X, and Y axes.
    - This is a MATRIX.
- Linear Algebra is the math you can do on POINTS, VECTORS, and MATRICES.

# Video Game Math

- Many linear algebra operations have geometric meaning:
  - Magnitude (length)
  - Weighted average (a.k.a. barycentric coords)
  - Dot product (Angle between vectors)
- To calculate magnitude, use the Pythagorean theorem
  - $\text{Length}(24,32) = \text{sqrt}(24 * 24 + 32 * 32)$   
 $= \text{sqrt}(1600)$   
 $= 40$

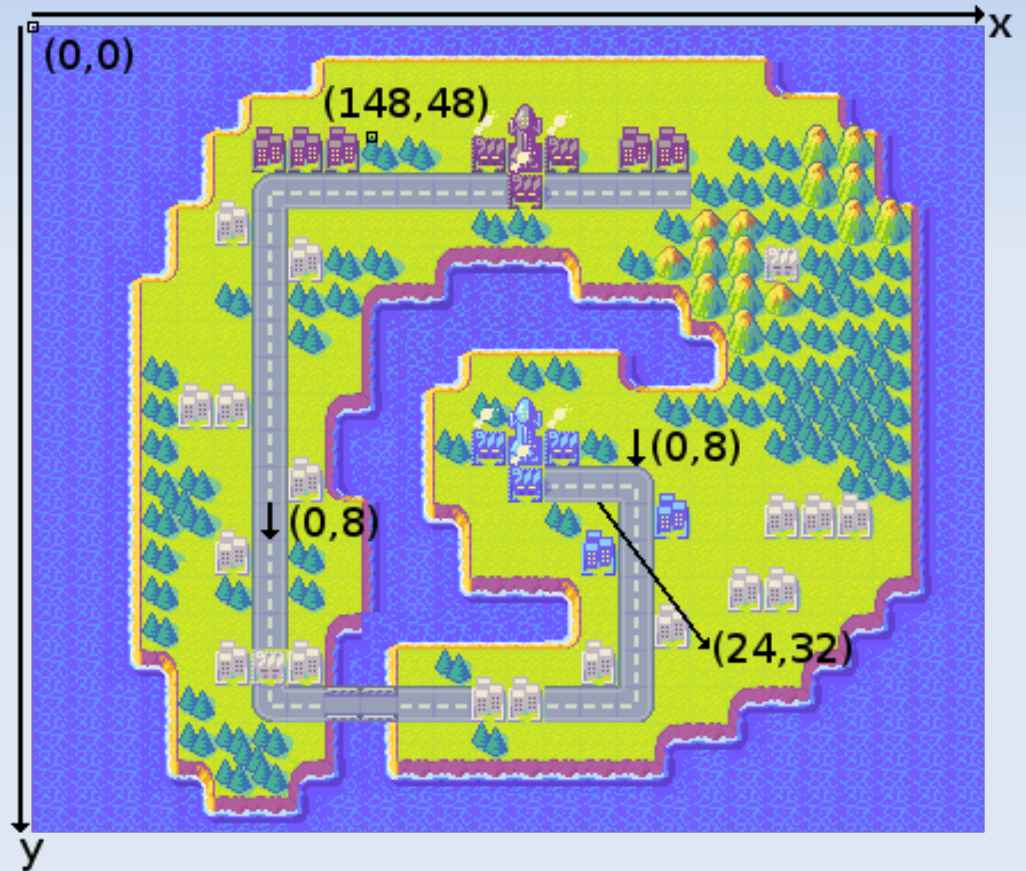


# Video Game Math

- To do a weighted average, do a bunch of scalar multiplies and adds that sum up to one
  - $0.2 * (24, 32) + 0.8 * (0, 8)$   
 $= (4.8, 6.4) + (0, 6.4)$
  - $= (4.8, 12.8)$
- To calculate dot product, multiply the X and Y parts together and add the result.
  - $\text{Dot}((24,32), (0,8)) = 24 * 0 + 32 * 8$   
 $= 256$

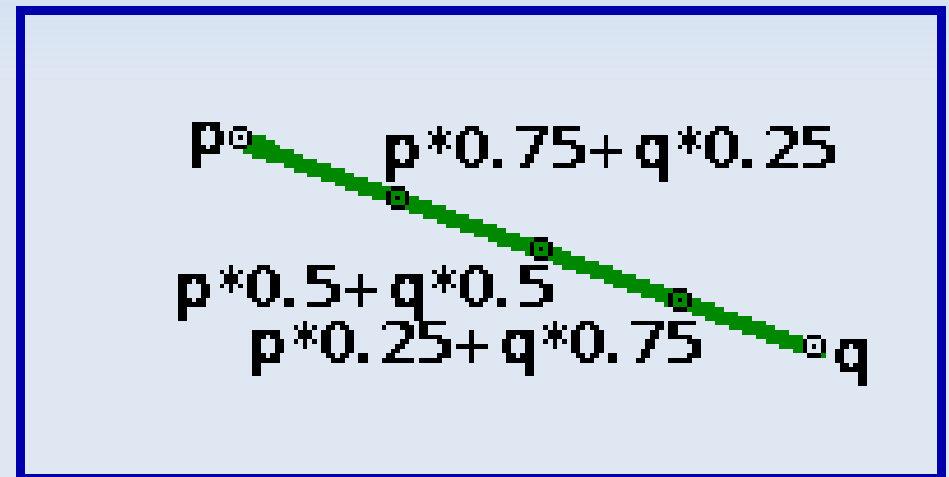
# Video Game Math

- Origin is upper left
- Points
  - Position in world
- Vector
  - Change in position



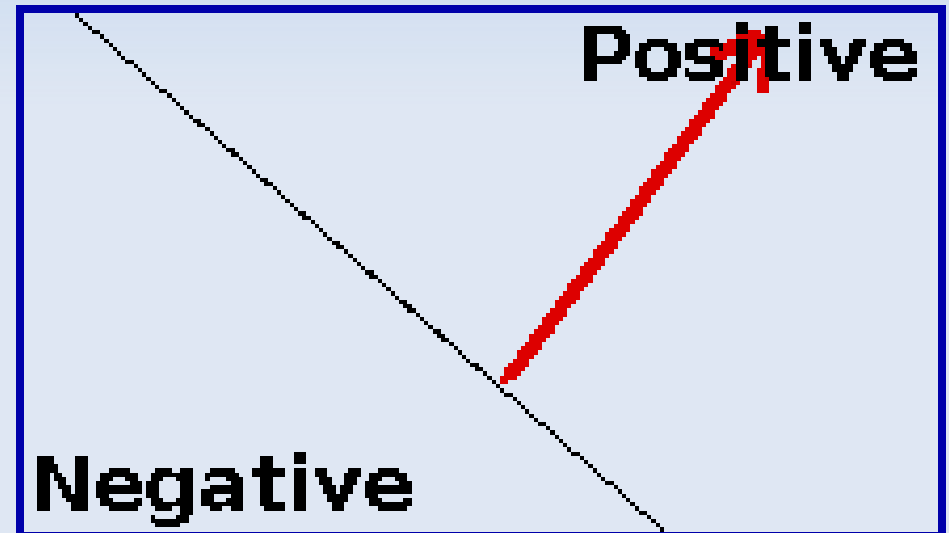
# Video Game Math

- Weighted Average
  - Has geometric meaning as long as weights add up to 1
- Animating this is called Linear Interpolation or "lerp"



# Video Game Math

- The dot product
- $v \cdot w = \text{Length}(v)$ 
  - \*  $\text{Length}(w)$
  - \*  $\cos \theta$
- If you look at the sign, you can see if two vectors are pointing in the same direction.



# Video Game Math

- Let's solve some real game problems:
  - Choose "direction" for animation to play.
  - Determine visibility in a stealth game.
  - Animate characters moving.

# Video Game Math



# Video Game Math





# Video Game Math



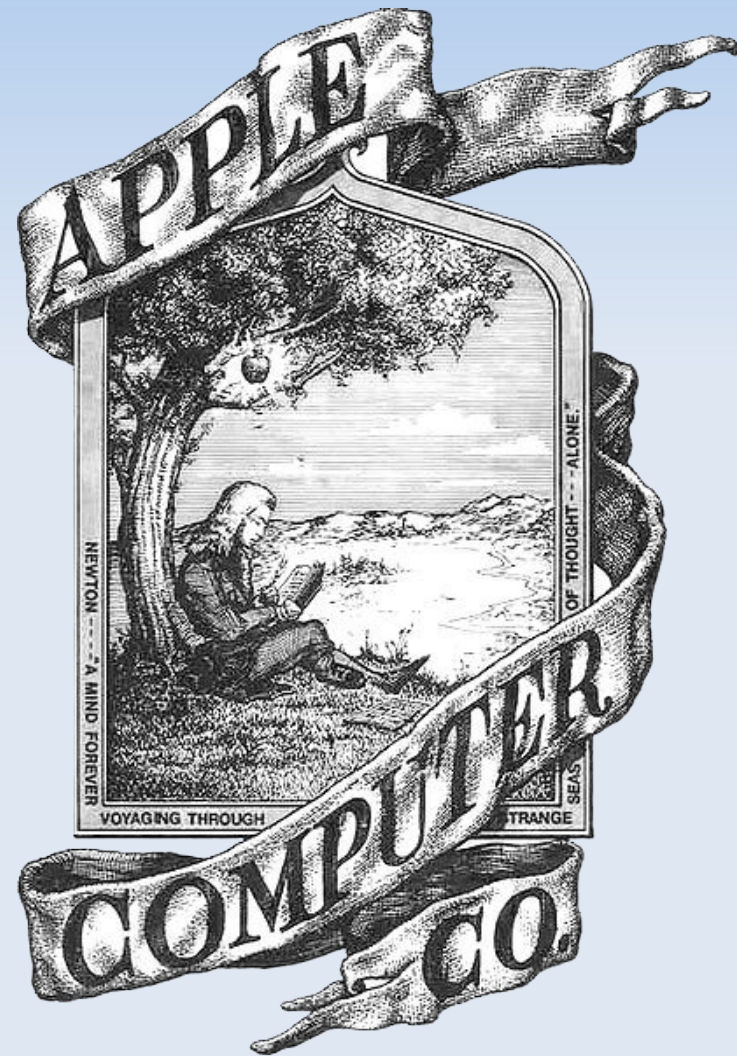


# Video Game Math

- What about Matrices and 3D?
- Matrices are generally not needed for 2D. They are extremely useful in 3D.
- Other useful 3D only things:
  - Cross product (perpendicular)
  - Determinant (volume)
  - "Left Hand" vs "Right Hand" coordinate systems

# Video Game Math

- And what about Calculus?
  - We will cover calculus when we get to video game physics.



# Video Game Math

- The math you will use is:
  - Algebra and Geometry
  - Trigonometry
  - Linear Algebra
- One nice thing about Linear Algebra is everything you will do has geometric interpretations.

# Video Game Math

Questions?

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